General Mathematics

18.01 Calculus
Prereq: None
U (Fall, Spring)
5-0-7 units. CALC I
Credit cannot also be received for 18.014, 18.01A, CC.181A, ES.1801, ES.181A


Fall: P. Seidel
Spring: Information: J. W. Bush

18.01A Calculus
Prereq: Knowledge of differentiation and elementary integration
U (Fall; first half of term)
5-0-7 units. CALC I
Credit cannot also be received for 18.01, 18.01A, CC.181A, ES.1801, ES.181A

Six-week review of one-variable calculus, emphasizing material not on the high-school AB syllabus: integration techniques and applications, improper integrals, infinite series, applications to other topics, such as probability and statistics, as time permits. Prerequisites: one year of high-school calculus or the equivalent, with a score of 4 or 5 on the AB Calculus test (or the AB portion of the BC test, or an equivalent score on a standard international exam), or equivalent college transfer credit, or a passing grade on the first half of the 18.01 advanced standing exam.

V. Gorin

18.014 Calculus with Theory
Prereq: None
U (Fall)
5-0-7 units. CALC I
Credit cannot also be received for 18.01, 18.01A, CC.181A, ES.1801, ES.181A

Covers the same material as 18.01, but at a deeper and more rigorous level. Emphasizes careful reasoning and understanding of proofs. Assumes knowledge of elementary calculus. Topics: axioms for the real numbers; the Riemann integral; limits, theorems on continuous functions; derivatives of functions of one variable; the fundamental theorems of calculus; Taylor's theorem; infinite series, power series, rigorous treatment of the elementary functions.

A. Pixton

18.02 Calculus
Prereq: Calculus I (GIR)
U (Fall, Spring)
5-0-7 units. CALC II
Credit cannot also be received for 18.022, 18.024, 18.02A, CC.1802, CC.182A, ES.1802, ES.182A

Calculus of several variables. Vector algebra in 3-space, determinants, matrices. Vector-valued functions of one variable, space motion. Scalar functions of several variables: partial differentiation, gradient, optimization techniques. Double integrals and line integrals in the plane; exact differentials and conservative fields; Green's theorem and applications, triple integrals, line and surface integrals in space, Divergence theorem, Stokes' theorem; applications.

Fall: J. W. Bush
Spring: G. Staffilani

18.02A Calculus
Prereq: Calculus I (GIR)
U (Fall, IAP, Spring)
5-0-7 units. CALC II
Credit cannot also be received for 18.02, 18.02A, CC.1802, CC.182A, ES.1802, ES.182A

First half is taught during the last six weeks of the Fall term; covers material in the first half of 18.02 (through double integrals). Second half of 18.02A can be taken either during IAP (daily lectures) or during the second half of the Spring term; it covers the remaining material in 18.02.

Fall: B. Hanin
Spring: Information: J. W. Bush
18.022 Calculus
Prereq: Calculus I (GIR)
U (Fall)
5-0-7 units. CALC II
Credit cannot also be received for 18.02, 18.024, 18.02A, CC.1802, CC.182A, ES.1802, ES.182A
Calculus of several variables. Topics as in 18.02 but with more focus on mathematical concepts. Vector algebra, dot product, matrices, determinant. Functions of several variables, continuity, differentiability, derivative. Parametrized curves, arc length, curvature, torsion. Vector fields, gradient, curl, divergence. Multiple integrals, change of variables, line integrals, surface integrals. Stokes' theorem in one, two, and three dimensions.
A. Borodin

18.024 Calculus with Theory
Prereq: Calculus I (GIR), permission of Instructor
U (Spring)
5-0-7 units. CALC II
Credit cannot also be received for 18.02, 18.022, 18.02A, CC.1802, CC.182A, ES.1802, ES.182A
Continues 18.014. Parallel to 18.02, but at a deeper level, emphasizing careful reasoning and understanding of proofs. Considerable emphasis on linear algebra and vector integral calculus.
J. Geiger

18.03 Differential Equations
Prereq: None. Coreq: Calculus II (GIR)
U (Fall, Spring)
5-0-7 units. REST
Credit cannot also be received for 18.034, CC.1803, ES.1803
Fall: J. Dunkel
Spring: D. Jerison, J. A. Kelner

18.031 System Functions and the Laplace Transform
Prereq: 18.03
U (IAP)
1-0-2 units
Studies basic continuous control theory as well as representation of functions in the complex frequency domain. Covers generalized functions, unit impulse response, and convolution; and Laplace transform, system (or transfer) function, and the pole diagram. Includes examples from mechanical and electrical engineering.
H. R. Miller, J. Orloff

18.034 Differential Equations
Prereq: None. Coreq: Calculus II (GIR)
U (Spring)
5-0-7 units. REST
Credit cannot also be received for 18.03, CC.1803, ES.1803
Covers much of the same material as 18.03 with more emphasis on theory. The point of view is rigorous and results are proven. Local existence and uniqueness of solutions.
P. Isett

18.04 Complex Variables with Applications
Prereq: Calculus II (GIR); 18.03 or 18.034
U (Fall)
4-0-8 units
Credit cannot also be received for 18.075, 18.0751
Complex algebra and functions; analyticity; contour integration, Cauchy's theorem; singularities, Taylor and Laurent series; residues, evaluation of integrals; multivalued functions, potential theory in two dimensions; Fourier analysis, Laplace transforms, and partial differential equations.
A. Nachbin

18.05 Introduction to Probability and Statistics
Prereq: Calculus I (GIR)
U (Spring)
4-0-8 units. REST
J. Orloff, D.A. Vogan
18.06 Linear Algebra
Prereq: Calculus II (GIR)
U (Fall, Spring)
4-0-8 units. REST
Credit cannot also be received for 18.700

Basic subject on matrix theory and linear algebra, emphasizing topics useful in other disciplines, including systems of equations, vector spaces, determinants, eigenvalues, singular value decomposition, and positive definite matrices. Applications to least-squares approximations, stability of differential equations, networks, Fourier transforms, and Markov processes. Uses MATLAB. Compared with 18.700, more emphasis on matrix algorithms and many applications.

Fall: A. Townsend
Spring: C. Barwick

18.062[J] Mathematics for Computer Science
Same subject as 6.042[J]
Prereq: Calculus I (GIR)
U (Fall, Spring)
5-0-7 units. REST
See description under subject 6.042[J].

F. T. Leighton, A. R. Meyer, A. Moitra

18.075 Methods for Scientists and Engineers
Subject meets with 18.0751
Prereq: Calculus II (GIR); 18.03
U (Spring)
3-0-9 units
Credit cannot also be received for 18.04

Covers functions of a complex variable; calculus of residues. Includes ordinary differential equations; Bessel and Legendre functions; Sturm-Liouville theory; partial differential equations; heat equation; and wave equations.

H. Cheng

18.0751 Methods for Scientists and Engineers
Subject meets with 18.075
Prereq: Calculus II (GIR); 18.03
G (Spring)
3-0-9 units
Credit cannot also be received for 18.04

Covers functions of a complex variable; calculus of residues. Includes ordinary differential equations; Bessel and Legendre functions; Sturm-Liouville theory; partial differential equations; heat equation; and wave equations. Students in Courses 6, 8, 12, 18, and 22 must register for undergraduate version, 18.075.

H. Cheng

18.085 Computational Science and Engineering I
Subject meets with 18.0851
Prereq: Calculus II (GIR); 18.03 or 18.034
U (Fall, Spring, Summer)
3-0-9 units

Review of linear algebra, applications to networks, structures, and estimation, finite difference and finite element solution of differential equations, Laplace’s equation and potential flow, boundary-value problems, Fourier series, discrete Fourier transform, convolution. Frequent use of MATLAB in a wide range of scientific and engineering applications.

Fall: P. Saenz
Spring: G. Strang

18.0851 Computational Science and Engineering I
Subject meets with 18.085
Prereq: Calculus II (GIR); 18.03 or 18.034
G (Fall, Spring, Summer)
3-0-9 units

Review of linear algebra, applications to networks, structures, and estimation, finite difference and finite element solution of differential equations, Laplace’s equation and potential flow, boundary-value problems, Fourier series, discrete Fourier transform, convolution. Frequent use of MATLAB in a wide range of scientific and engineering applications. Students in Course 18 must register for the undergraduate version, 18.085.

Fall: P. Saenz
Spring: G. Strang

18.086 Computational Science and Engineering II
Subject meets with 18.086
Prereq: Calculus II (GIR); 18.03 or 18.034
U (Spring)
3-0-9 units


N. Stoop
18.0861 Computational Science and Engineering II
Subject meets with 18.086
Prereq: Calculus II (GIR); 18.03 or 18.034
G (Spring)
3-0-9 units

Initial value problems: finite difference methods, accuracy and
stability, heat equation, wave equations, conservation laws and
shocks, level sets, Navier-Stokes. Solving large systems: elimination
with reordering, iterative methods, preconditioning, multigrid,
Krylov subspaces, conjugate gradients. Optimization and minimum
principles: weighted least squares, constraints, inverse problems,
calculus of variations, saddle point problems, linear programming,
duality, adjoint methods. Students in Course 18 must register for the
undergraduate version, 18.086.
N. Stoop

18.089 Review of Mathematics
Prereq: Permission of instructor
G (Summer)
5-0-7 units

One-week review of one-variable calculus (18.01), followed by
concentrated study covering multivariable calculus (18.02), two
hours per day for five weeks. Primarily for graduate students in
Course 2N. Degree credit allowed only in special circumstances.
Information: J. W. Bush

18.094[J] Teaching College-Level Science and Engineering
Same subject as 1.95[J], 5.95[J], 6.982[J], 7.59[J], 8.395[J]
Subject meets with 2.978
Prereq: None
G (Fall)
2-0-2 units

See description under subject 5.95[J].
J. Rankin

18.095 Mathematics Lecture Series
Prereq: Calculus I (GIR)
U (IAP)
2-0-4 units
Can be repeated for credit.

Ten lectures by mathematics faculty members on interesting
topics from both classical and modern mathematics. All lectures
accessible to students with calculus background and an interest in
mathematics. At each lecture, reading and exercises are assigned.
Students prepare these for discussion in a weekly problem session.
Information: J. W. Bush

18.098 Independent Study
Prereq: Permission of instructor
U (Fall, IAP, Spring)
Units arranged [P/D/F]
Can be repeated for credit.

Studies or special individual reading arranged in consultation with
individual faculty members and subject to departmental approval.
Information: J. W. Bush

18.099 Independent Study
Prereq: Permission of instructor
U (Fall, IAP, Spring, Summer)
Units arranged
Can be repeated for credit.

Studies (during IAP) or special individual reading (during regular
terms). Arranged in consultation with individual faculty members
and subject to departmental approval.
Information: J. W. Bush

Analysis

18.1001 Real Analysis
Subject meets with 18.100A
Prereq: Calculus II (GIR); or 18.014 and Coreq: Calculus II (GIR)
G (Fall, Spring)
3-0-9 units
Credit cannot also be received for 18.100B, 18.100C

Three options offered, each covering fundamentals of mathematical
analysis: convergence of sequences and series, continuity,
derivativeability, Riemann integral, sequences and series of
functions, uniformity, interchange of limit operations. Each option
shows the utility of abstract concepts and teaches understanding
and construction of proofs. Option A: Proofs and definitions are less
abstract. Gives applications where possible. Concerned primarily
with the real line. Option B: More demanding; for students with more
mathematical maturity. Places more emphasis on point-set topology
and n-space. Option C: 15-unit (4-0-11) variant of Option B, with
further instruction and practice in written communication. Students
in Course 18 must register for one of the undergraduate versions of
this subject: 18.100A, 18.100B, or 18.100C.
Fall: A. P. Mattuck
Spring: T. Beck
18.1002 Real Analysis
Subject meets with 18.100B
Prereq: Calculus II (GIR); or 18.014 and Coreq: Calculus II (GIR)
G (Fall, Spring)
3-0-9 units
Credit cannot also be received for 18.100A, 18.100C

Three options offered, each covering fundamentals of mathematical analysis: convergence of sequences and series, continuity, differentiability, Riemann integral, sequences and series of functions, uniformity, interchange of limit operations. Each option shows the utility of abstract concepts and teaches understanding and construction of proofs. Option A: Proofs and definitions are less abstract. Gives applications where possible. Concerned primarily with the real line. Option B: More demanding; for students with more mathematical maturity. Places more emphasis on point-set topology and n-space. Option C: 15-unit (4-0-11) variant of Option B, with further instruction and practice in written communication. Students in Course 18 must register for one of the undergraduate versions of this subject: 18.100A, 18.100B, or 18.100C.

Fall: P. Isett
Spring: J. Zahl

18.100A Real Analysis
Subject meets with 18.1001
Prereq: Calculus II (GIR); or 18.014 and Coreq: Calculus II (GIR)
U (Fall, Spring)
3-0-9 units
Credit cannot also be received for 18.100B, 18.100C

18.100B Real Analysis
Subject meets with 18.1002
Prereq: Calculus II (GIR); or 18.014 and Coreq: Calculus II (GIR)
U (Fall, Spring)
3-0-9 units
Credit cannot also be received for 18.100A, 18.100C

18.100C Real Analysis
Prereq: Calculus II (GIR); or 18.014 and Coreq: Calculus II (GIR)
U (Fall, Spring)
4-0-11 units
Credit cannot also be received for 18.1001, 18.1002, 18.100A, 18.100B

Three options offered, each covering fundamentals of mathematical analysis: convergence of sequences and series, continuity, differentiability, Riemann integral, sequences and series of functions, uniformity, interchange of limit operations. Each option shows the utility of abstract concepts and teaches understanding and construction of proofs. Option A: Proofs and definitions are less abstract. Gives applications where possible. Concerned primarily with the real line. Option B: More demanding; for students with more mathematical maturity. Places more emphasis on point-set topology and n-space. Option C: 15-unit (4-0-11) variant of Option B, with further instruction and practice in written communication. Fall: 18.100A: A. P. Mattuck
18.100B: P. Isett
18.100C: E. Murphy
Spring: 18.100A: T. Beck
18.100B: J. Zahl
18.100C: S. Seyfaddini

18.101 Analysis and Manifolds
Subject meets with 18.1011
Prereq: 18.100A, 18.100B, or 18.100C; 18.06, 18.700, or 18.701
U (Fall)
3-0-9 units

Introduction to the theory of manifolds: vector fields and densities on manifolds, integral calculus in the manifold setting and the manifold version of the divergence theorem. 18.901 helpful but not required. V. W. Guillemin

18.1011 Analysis and Manifolds
Subject meets with 18.101
Prereq: 18.100A, 18.100B, or 18.100C; 18.06, 18.700, or 18.701
G (Fall)
3-0-9 units

Introduction to the theory of manifolds: vector fields and densities on manifolds, integral calculus in the manifold setting and the manifold version of the divergence theorem. 18.901 helpful but not required. Students in Course 18 must register for the undergraduate version, 18.101. V. W. Guillemin
18.102 Introduction to Functional Analysis
Subject meets with 18.1021
Prereq: 18.100A, 18.100B, or 18.100C; 18.06, 18.700, or 18.701
U (Spring)
3-0-9 units
R. B. Melrose

18.1021 Introduction to Functional Analysis
Subject meets with 18.102
Prereq: 18.100A, 18.100B, or 18.100C; 18.06, 18.700, or 18.701
G (Spring)
3-0-9 units
Students in Course 18 must register for the undergraduate version, 18.102.
R. B. Melrose

18.103 Fourier Analysis: Theory and Applications
Subject meets with 18.1031
Prereq: 18.100A, 18.100B, or 18.100C; 18.06, 18.700, or 18.701
U (Fall)
3-0-9 units
Roughly half the subject devoted to the theory of the Lebesgue integral with applications to probability, and half to Fourier series and Fourier integrals.
L. Guth

18.1031 Fourier Analysis: Theory and Applications
Subject meets with 18.103
Prereq: 18.100A, 18.100B, or 18.100C; 18.06, 18.700, or 18.701
G (Fall)
3-0-9 units
Roughly half the subject devoted to the theory of the Lebesgue integral with applications to probability, and half to Fourier series and Fourier integrals. Students in Course 18 must register for the undergraduate version, 18.103.
L. Guth

18.104 Seminar in Analysis
Prereq: 18.100A, 18.100B, or 18.100C
U (Spring)
3-0-9 units
Students present and discuss material from books or journals. Topics vary from year to year. Instruction and practice in written and oral communication provided.
G. Staffilani

18.112 Functions of a Complex Variable
Subject meets with 18.1121
Prereq: 18.100A, 18.100B, or 18.100C; 18.06, 18.700, or 18.701
U (Fall)
3-0-9 units
H. Krieger

18.1121 Functions of a Complex Variable
Subject meets with 18.112
Prereq: 18.100A, 18.100B, or 18.100C; 18.06, 18.700, or 18.701
G (Fall)
3-0-9 units
H. Krieger
18.116 Riemann Surfaces
Prereq: 18.112
Acad Year 2016-2017: G (Spring)
Acad Year 2017-2018: Not offered
3-0-9 units
Riemann surfaces, uniformization, Riemann-Roch Theorem. Theory of elliptic functions and modular forms. Some applications, such as to number theory.
T. S. Mrowka

18.117 Topics in Several Complex Variables
Prereq: 18.112, 18.965
Acad Year 2016-2017: G (Spring)
Acad Year 2017-2018: Not offered
3-0-9 units
Can be repeated for credit.
Harmonic theory on complex manifolds, Hodge decomposition theorem, Hard Lefschetz theorem. Vanishing theorems. Theory of Stein manifolds. As time permits students also study holomorphic vector bundles on Kahler manifolds.
V. W. Guillemin

18.125 Measure Theory and Analysis
Prereq: 18.100A, 18.100B, or 18.100C
G (Spring)
3-0-9 units
Provides a rigorous introduction to Lebesgue’s theory of measure and integration. Covers material that is essential in analysis, probability theory, and differential geometry.
S. Dyatlov

18.137 Topics in Geometric Partial Differential Equations
Prereq: Permission of Instructor
Acad Year 2016-2017: Not offered
Acad Year 2017-2018: G (Spring)
3-0-9 units
Can be repeated for credit.
Topics vary from year to year.
W. Minicozzi

18.152 Introduction to Partial Differential Equations
Subject meets with 18.1521
Prereq: 18.100A, 18.100B, or 18.100C; 18.06, 18.700, or 18.701
Acad Year 2016-2017: Not offered
Acad Year 2017-2018: U (Spring)
3-0-9 units
Introduces three main types of partial differential equations: diffusion, elliptic, and hyperbolic. Includes mathematical tools, real-world examples and applications, such as the Black-Scholes equation, the European options problem, water waves, scalar conservation laws, first order equations and traffic problems.
T. Walpuski

18.1521 Introduction to Partial Differential Equations
Subject meets with 18.152
Prereq: 18.100A, 18.100B, or 18.100C; 18.06, 18.700, or 18.701
Acad Year 2016-2017: Not offered
Acad Year 2017-2018: G (Spring)
3-0-9 units
Introduces three main types of partial differential equations: diffusion, elliptic, and hyperbolic. Includes mathematical tools, real-world examples and applications, such as the Black-Scholes equation, the European options problem, water waves, scalar conservation laws, first order equations and traffic problems. Students in Course 18 must register for the undergraduate version, 18.152.
T. Walpuski

18.155 Differential Analysis I
Prereq: 18.102 or 18.103
G (Fall)
3-0-9 units

18.156 Differential Analysis II
Prereq: 18.155
G (Spring)
3-0-9 units
Spring: Variable coefficient elliptic, parabolic and hyperbolic partial differential equations. 18.112 recommended for 18.155.
Fall: R. B. Melrose
Spring: L. Guth
18.157 Introduction to Microlocal Analysis
Prereq: 18.155
Acad Year 2016-2017: G (Spring)
Acad Year 2017-2018: Not offered
3-0-9 units

The semi-classical theory of partial differential equations. Discussion of Pseudodifferential operators, Fourier integral operators, asymptotic solutions of partial differential equations, and the spectral theory of Schrödinger operators from the semi-classical perspective. Heavy emphasis placed on the symplectic geometric underpinnings of this subject.

R. B. Melrose

18.158 Topics in Differential Equations
Prereq: 18.157
Acad Year 2016-2017: Not offered
Acad Year 2017-2018: G (Fall, Spring)
3-0-9 units
Can be repeated for credit.

Topics vary from year to year.
Fall: D. Jerison
Spring: Information: G. Staffilani

18.175 Theory of Probability
Prereq: 18.100A, 18.100B, or 18.100C
G (Spring)
3-0-9 units

Sums of independent random variables, central limit phenomena, infinitely divisible laws, Levy processes, Brownian motion, conditioning, and martingales. Prior exposure to probability (e.g., 18.600) recommended.

V. Gorin

18.176 Stochastic Calculus
Prereq: 18.175
Acad Year 2016-2017: Not offered
Acad Year 2017-2018: G (Spring)
3-0-9 units

Introduction to stochastic processes with an emphasis on their relationship to other branches of analysis, especially partial differential equations. Topics include Brownian motion, continuous parameter martingales, Ito's theory of stochastic differential equations, Levy processes, and may also address Malliavin's calculus. Students should have familiarity with Lebesgue integration and its application to probability, as well knowledge of the Fourier transform and other basic tools of analysis.

D. W. Stroock

18.177 Topics in Stochastic Processes
Prereq: 18.175
G (Fall)
3-0-9 units
Can be repeated for credit.

Topics vary from year to year.
S. Sheffield

18.199 Graduate Analysis Seminar
Prereq: Permission of instructor
Acad Year 2016-2017: G (Fall)
Acad Year 2017-2018: Not offered
3-0-9 units
Can be repeated for credit.

Studies original papers in differential analysis and differential equations. Intended for first- and second-year graduate students. Permission must be secured in advance.

V. W. Guillemin

Discrete Applied Mathematics

18.200 Principles of Discrete Applied Mathematics
Prereq: Calculus II (GIR)
U (Fall)
4-0-11 units
Credit cannot also be received for 18.200A

Study of illustrative topics in discrete applied mathematics, including sorting algorithms, probability theory, information theory, coding theory, secret codes, generating functions, and linear programming. Instruction and practice in written communication provided.

A. Moitra, P. W. Shor

18.200A Principles of Discrete Applied Mathematics
Prereq: Calculus II (GIR)
U (Spring)
3-0-9 units
Credit cannot also be received for 18.200

Study of illustrative topics in discrete applied mathematics, including sorting algorithms, probability theory, information theory, coding theory, secret codes, generating functions, and linear programming.

M. X. Goemans
18.204 Undergraduate Seminar in Discrete Mathematics
Prereq: 18.200 or 18.062[J]; 18.06, 18.700, or 18.701; or permission of instructor
U (Fall, Spring)
3-0-9 units
Credit cannot also be received for 18.219
Seminar in combinatorics, graph theory, and discrete mathematics in general. Participants read and present papers from recent mathematics literature. Instruction and practice in written and oral communication provided. Enrollment limited.
Fall: T. McConville
Spring: Information: J. W. Bush

18.211 Combinatorial Analysis
Prereq: Calculus II (GIR); 18.06, 18.700, or 18.701
U (Fall)
3-0-9 units
Combinatorial problems and methods for their solution. Enumeration, generating functions, recurrence relations, construction of bijections. Introduction to graph theory. Prior experience with abstraction and proofs is helpful.
P. Csikvari

18.212 Algebraic Combinatorics
Prereq: 18.701 or 18.703
U (Spring)
3-0-9 units
Applications of algebra to combinatorics. Topics include walks in graphs, the Radon transform, groups acting on posets, Young tableaux, electrical networks.
P. Csikvari

18.217 Combinatorial Theory
Prereq: Permission of instructor
G (Fall)
3-0-9 units
Can be repeated for credit.
Content varies from year to year.
R. P. Stanley

18.218 Topics in Combinatorics
Prereq: Permission of instructor
G (Spring)
3-0-9 units
Can be repeated for credit.
Topics vary from year to year.
A. Postnikov

18.219 Seminar in Combinatorics
Prereq: Permission of instructor
Acad Year 2016-2017: G (Fall)
Acad Year 2017-2018: Not offered
3-0-9 units
Can be repeated for credit. Credit cannot also be received for 18.204
Content varies from year to year. Readings from current research papers in combinatorics. Topics to be chosen and presented by the class.
J. Fox

Continuous Applied Mathematics

18.300 Principles of Continuum Applied Mathematics
Prereq: Calculus II (GIR); 18.03 or 18.034
U (Spring)
3-0-9 units
Covers fundamental concepts in continuous applied mathematics. Applications from traffic flow, fluids, elasticity, granular flows, etc. Also covers continuum limit; conservation laws, quasi-equilibrium; kinematic waves; characteristics, simple waves, shocks; diffusion (linear and nonlinear); numerical solution of wave equations; finite differences, consistency, stability; discrete and fast Fourier transforms; spectral methods; transforms and series (Fourier, Laplace). Additional topics may include sonic booms, Mach cone, caustics, lattices, dispersion and group velocity. Uses MATLAB computing environment.
L. Faria

18.303 Linear Partial Differential Equations: Analysis and Numerics
Prereq: 18.06 or 18.700
U (Fall)
3-0-9 units
Provides students with the basic analytical and computational tools of linear partial differential equations (PDEs) for practical applications in science and engineering, including heat/diffusion, wave, and Poisson equations. Analytics emphasize the viewpoint of linear algebra and the analogy with finite matrix problems. Studies operator adjoints and eigenproblems, series solutions, Green’s functions, and separation of variables. Numerics focus on finite-difference and finite-element techniques to reduce PDEs to matrix problems, including stability and convergence analysis and implicit/explicit timestepping. MATLAB is introduced and used in homework for simple examples.
S. G. Johnson
18.305 Advanced Analytic Methods in Science and Engineering
Prereq: 18.04, 18.075, or 18.112
G (Fall)
3-0-9 units
Covers expansion around singular points: the WKB method on ordinary and partial differential equations; the method of stationary phase and the saddle point method; the two-scale method and the method of renormalized perturbation; singular perturbation and boundary-layer techniques; WKB method on partial differential equations.
H. Reid

18.306 Advanced Partial Differential Equations with Applications
Prereq: 18.03 or 18.034; 18.04, 18.075, or 18.112
G (Spring)
3-0-9 units
A. Nachbin

18.327 Topics in Applied Mathematics
Prereq: Permission of instructor
Acad Year 2016-2017: G (Fall)
Acad Year 2017-2018: Not offered
3-0-9 units
Can be repeated for credit.
Topics vary from year to year.
L. Demanet

18.330 Introduction to Numerical Analysis
Prereq: Calculus II (GIR); 18.03 or 18.034
U (Spring)
3-0-9 units
H. Reid

18.335[J] Introduction to Numerical Methods
Same subject as 6.337[J]
Prereq: 18.03 or 18.034; 18.06, 18.700, or 18.701
G (Spring)
3-0-9 units
Advanced introduction to numerical linear algebra and other central algorithms of scientific computation. Topics include direct and iterative methods for linear systems, eigenvalue and QR/SVD factorizations, stability and accuracy, floating-point arithmetic, sparse matrices, preconditioning, and the memory considerations underlying modern linear-algebra software. Techniques for local and global nonlinear optimization, including quasi-Newton methods, trust regions, branch-and-bound, and multistart algorithms. Chebyshev approximations, numerical integration, and FFTs. A modern high-level language, Julia, is introduced for problem sets.
W. Shin

Same subject as 6.335[J]
Prereq: 6.336[J], 16.920[J], 18.085, 18.335[J], or permission of instructor
G (Fall)
3-0-9 units
Unified introduction to the theory and practice of modern, near linear-time, numerical methods for large-scale partial-differential and integral equations. Topics include preconditioned iterative methods; generalized Fast Fourier Transform and other butterfly-based methods; multiresolution approaches, such as multigrid algorithms and hierarchical low-rank matrix decompositions; and low and high frequency Fast Multipole Methods. Example applications include aircraft design, cardiovascular system modeling, electronic structure computation, and tomographic imaging.
A. Townsend
18.337[J] Parallel Computing
Same subject as 6.338[J]
Prereq: 18.06, 18.700, or 18.701
G (Fall)
3-0-9 units
Interdisciplinary introduction to computing with Julia. Covers scientific computing and data analysis problems. Combines knowledge from computer science and computational science illustrating Julia’s new approach to scientific computing. Sample scientific computing topics include dense and sparse linear algebra, Fourier transforms, data handling, and N-body problems. Provides direct experience with programming traditional-style supercomputing as well as working with modern cloud computing stacks.
A. Edelman

18.338 Eigenvalues of Random Matrices
Prereq: 18.701 or permission of instructor
Acad Year 2016-2017: Not offered
Acad Year 2017-2018: G (Spring)
3-0-9 units
Covers the modern main results of random matrix theory as it is currently applied in engineering and science. Topics include matrix calculus for finite and infinite matrices (e.g., Wigner’s semi-circle and Marcenko-Pastur laws), free probability, random graphs, combinatorial methods, matrix statistics, stochastic operators, passage to the continuum limit, moment methods, and compressed sensing. Knowledge of MATLAB helpful, but not required.
A. Edelman

18.352[J] Theoretical Environmental Analysis
Same subject as 12.009[J]
Prereq: Physics I (GIR), Calculus II (GIR); Coreq: 18.03
U (Spring)
3-0-9 units
See description under subject 12.009[J].
D. H. Rothman

18.353[J] Nonlinear Dynamics: Chaos
Same subject as 2.050[J], 12.006[J]
Prereq: 18.03 or 18.034; Physics II (GIR)
U (Fall)
3-0-9 units
See description under subject 12.006[J].
P-T. Brun

18.354[J] Nonlinear Dynamics: Continuum Systems
Same subject as 1.062[J], 12.207[J]
Subject meets with 18.3541
Prereq: 18.03 or 18.034; Physics II (GIR)
U (Spring)
3-0-9 units
General mathematical principles of continuum systems. From microscopic to macroscopic descriptions in the form of linear or nonlinear (partial) differential equations. Exact solutions, dimensional analysis, calculus of variations and singular perturbation methods. Stability, waves and pattern formation in continuum systems. Subject matter illustrated using natural fluid and solid systems found, for example, in geophysics and biology.
L. Bourouiba

18.3541 Nonlinear Dynamics: Continuum Systems
Subject meets with 1.062[J], 12.207[J], 18.354[J]
Prereq: 18.03 or 18.034; Physics II (GIR)
G (Spring)
3-0-9 units
General mathematical principles of continuum systems. From microscopic to macroscopic descriptions in the form of linear or nonlinear (partial) differential equations. Exact solutions, dimensional analysis, calculus of variations and singular perturbation methods. Stability, waves and pattern formation in continuum systems. Subject matter illustrated using natural fluid and solid systems found, for example, in geophysics and biology. Students in Courses 1, 12, and 18 must register for undergraduate version, 18.354[J].
L. Bourouiba

18.355 Fluid Mechanics
Prereq: 18.354[J], 2.25, or 12.800
Acad Year 2016-2017: G (Fall)
Acad Year 2017-2018: Not offered
3-0-9 units
Topics include the development of Navier-Stokes equations, inviscid flows, boundary layers, lubrication theory, Stokes flows, and surface tension. Fundamental concepts illustrated through problems drawn from a variety of areas, including geophysics, biology, and the dynamics of sport. Particular emphasis on the interplay between dimensional analysis, scaling arguments, and theory. Includes classroom and laboratory demonstrations.
J. W. Bush
18.357 Interfacial Phenomena  
Prereq: 18.354[J], 18.355, 12.800, 2.25, or permission of instructor  
Acad Year 2016-2017: Not offered  
Acad Year 2017-2018: G (Spring)  
3-0-9 units  
Fluid systems dominated by the influence of interfacial tension.  
Elucidates the roles of curvature pressure and Marangoni stress in  
a variety of hydrodynamic settings. Particular attention to drops  
and bubbles, soap films and minimal surfaces, wetting phenomena,  
water-repellency, surfactants, Marangoni flows, capillary  
origami and contact line dynamics. Theoretical developments are  
accompanied by classroom demonstrations. Highlights the role of  
surface tension in biology.  
J. W. Bush

18.369 Mathematical Methods in Nanophotonics  
Prereq: 18.305 or permission of instructor  
Acad Year 2016-2017: Not offered  
Acad Year 2017-2018: G (Spring)  
3-0-9 units  
High-level approaches to understanding complex optical media,  
structured on the scale of the wavelength, that are not generally  
analytically solvable. The basis for understanding optical  
phenomena such as photonic crystals and band gaps, anomalous  
diffraction, mechanisms for optical confinement, optical fibers (new  
and old), nonlinearities, and integrated optical devices. Methods  
covered include linear algebra and eigensystems for Maxwell's  
equations, symmetry groups and representation theory, Bloch's  
theorem, numerical eigensolver methods, time and frequency-  
domain computation, perturbation theory, and coupled-mode  
theories.  
S. G. Johnson

18.376[J] Wave Propagation  
Same subject as 1.138[J], 2.062[J]  
Prereq: 2.003[J], 18.075  
G (Spring)  
3-0-9 units  
See description under subject 2.062[J].  
T. R. Akylas, R. R. Rosales

18.377[J] Nonlinear Dynamics and Waves  
Same subject as 1.685[J], 2.034[J]  
Prereq: Permission of instructor  
Acad Year 2016-2017: G (Spring)  
Acad Year 2017-2018: Not offered  
3-0-9 units  
A unified treatment of nonlinear oscillations and wave phenomena  
with applications to mechanical, optical, geophysical, fluid,  
electrical and flow-structure interaction problems. Nonlinear  
free and forced vibrations; nonlinear resonances; self-excited  
oscillations; lock-in phenomena. Nonlinear dispersive and  
nondispersive waves; resonant wave interactions; propagation of  
wave pulses and nonlinear Schrodinger equation. Nonlinear long  
waves and breaking; theory of characteristics; the Korteweg-de Vries  
equation; solitons and solitary wave interactions. Stability of shear  
flows. Some topics and applications may vary from year to year.  
T. R. Akylas, R. R. Rosales

18.384 Undergraduate Seminar in Physical Mathematics  
Prereq: 18.300, 18.353[J], 18.354[J], or permission of instructor  
U (Spring)  
3-0-9 units  
Covers the mathematical modeling of physical systems, with  
emphasis on the reading and presentation of papers. Addresses  
a broad range of topics, with particular focus on macroscopic  
physics and continuum systems: fluid dynamics, solid mechanics,  
and biophysics. Instruction and practice in written and oral  
communication provided.  
M. Brenner

18.385[J] Nonlinear Dynamics and Chaos  
Same subject as 2.036[J]  
Prereq: 18.03 or 18.034  
Acad Year 2016-2017: G (Fall)  
Acad Year 2017-2018: Not offered  
3-0-9 units  
Introduction to the theory of nonlinear dynamical systems with  
applications from science and engineering. Local and global  
existence of solutions, dependence on initial data and parameters.  
Elementary bifurcations, normal forms. Phase plane, limit cycles,  
relaxation oscillations, Poincare-Bendixson theory. Floquet  
Synchronization. Introduction to chaos. Universality. Strange  
 Attractors. Lorenz and Rossler systems. Hamiltonian dynamics and  
KAM theory. Uses MATLAB computing environment.  
R. R. Rosales
18.395 Group Theory with Applications to Physics
Prereq: 8.321
G (Fall)
Not offered regularly; consult department
3-0-9 units
Selection of topics from the theory of finite groups, Lie groups, and group representations, motivated by quantum mechanics and particle physics. 8.322 and 8.323 helpful.
D. Z. Freedman

18.396[J] Supersymmetric Quantum Field Theories
Same subject as 8.831[J]
Prereq: Permission of instructor
G (Fall)
Not offered regularly; consult department
3-0-9 units
Can be repeated for credit.
Topics selected from the following: SUSY algebras and their particle representations; Weyl and Majorana spinors; Lagrangians of basic four-dimensional SUSY theories, both rigid SUSY and supergravity; supermultiplets of fields and superspace methods; renormalization properties, and the non-renormalization theorem; spontaneous breakdown of SUSY; and phenomenological SUSY theories. Some prior knowledge of Noether's theorem, derivation and use of Feynman rules, l-loop renormalization, and gauge theories is essential.
D. Z. Freedman

18.400[J] Automata, Computability, and Complexity
Same subject as 6.045[J]
Prereq: 6.042[J]
U (Spring)
4-0-8 units
See description under subject 6.045[J].
S. Aaronson

Theoretical Computer Science

18.404 Theory of Computation
Subject meets with 6.840[J], 18.4041[J]
Prereq: 18.200 or 18.062[J]
U (Fall)
4-0-8 units
A more extensive and theoretical treatment of the material in 6.045[J]/18.400[J], emphasizing computability and computational complexity theory. Regular and context-free languages. Decidable and undecidable problems, reducibility, recursive function theory. Time and space measures on computation, completeness, hierarchy theorems, inherently complex problems, oracles, probabilistic computation, and interactive proof systems.
M. Sipser

18.4041[J] Theory of Computation
Same subject as 6.840[J]
Subject meets with 18.404
Prereq: 18.200 or 18.062[J]
G (Fall)
4-0-8 units
A more extensive and theoretical treatment of the material in 6.045[J]/18.400[J], emphasizing computability and computational complexity theory. Regular and context-free languages. Decidable and undecidable problems, reducibility, recursive function theory. Time and space measures on computation, completeness, hierarchy theorems, inherently complex problems, oracles, probabilistic computation, and interactive proof systems. Students in Course 18 must register for the undergraduate version, 18.404.
M. Sipser

18.405[J] Advanced Complexity Theory
Same subject as 6.841[J]
Prereq: 18.404
Acad Year 2016-2017: Not offered
Acad Year 2017-2018: G (Spring)
3-0-9 units
D. Moshkovitz
18.408 Topics in Theoretical Computer Science
Prereq: Permission of instructor
Acad Year 2016-2017: G (Spring)
Acad Year 2017-2018: Not offered
3-0-9 units
Can be repeated for credit.
Study of areas of current interest in theoretical computer science.
Topics vary from term to term.
A. Moitra

18.410[J] Design and Analysis of Algorithms
Same subject as 6.046[J]
Prereq: 6.006
U (Fall, Spring)
4-0-8 units
See description under subject 6.046[J].
E. Demaine, M. Goemans

18.415[J] Advanced Algorithms
Same subject as 6.854[J]
Prereq: 6.041, 6.042[J], or 18.600; 6.046[J]
Acad Year 2016-2017: Not offered
Acad Year 2017-2018: G (Spring)
5-0-7 units
See description under subject 6.854[J].
A. Moitra, D. R. Karger

18.416[J] Randomized Algorithms
Same subject as 6.856[J]
Prereq: 6.041, 6.042[J], or 18.600; 6.046[J]
Acad Year 2016-2017: Not offered
Acad Year 2017-2018: G (Spring)
5-0-7 units
See description under subject 6.856[J].
D. R. Karger

18.417 Introduction to Computational Molecular Biology
Prereq: 6.01, 6.006, or permission of instructor
G (Fall)
Not offered regularly; consult department
3-0-9 units
Introduces the basic computational methods used to model and
predict the structure of biomolecules (proteins, DNA, RNA). Covers
classical techniques in the field (molecular dynamics, Monte Carlo,
dynamic programming) to more recent advances in analyzing and
predicting RNA and protein structure, ranging from Hidden Markov
Models and 3-D lattice models to attribute Grammars and tree
Grammars.
Information: B. Berger

18.418 Topics in Computational Molecular Biology
Prereq: 18.417, 6.047, or permission of instructor
G (Spring)
3-0-9 units
Can be repeated for credit.
Covers current research topics in computational molecular biology.
Recent research papers presented from leading conferences such
as the SIGACT International Conference on Computational Molecular
Biology (RECOMB). Topics include original research (both theoretical
and experimental) in comparative genomics, sequence and structure
analysis, molecular evolution, proteomics, gene expression,
transcriptional regulation, and biological networks. Recent research
by course participants also covered. Participants will be expected to
present either group or individual projects to the class.
B. Berger

18.424 Seminar in Information Theory
Prereq: 18.05, 18.600, or 6.041; 18.06, 18.700, or 18.701
U (Spring)
3-0-9 units
Considers various topics in information theory, including data
compression, Shannon’s Theorems, and error-correcting codes.
Students present and discuss the subject matter. Instruction and
practice in written and oral communication provided.
P. W. Shor

18.425[J] Cryptography and Cryptanalysis
Same subject as 6.875[J]
Prereq: 6.046[J]
G (Spring)
3-0-9 units
See description under subject 6.875[J].
S. Goldwasser, S. Micali

18.434 Seminar in Theoretical Computer Science
Prereq: 18.410[J]
U (Spring)
3-0-9 units
Topics vary from year to year. Students present and discuss
the subject matter. Instruction and practice in written and oral
communication provided.
Y. Zhou
18.435[J] Quantum Computation
Same subject as 2.111[J], 8.370[J]
Prereq: Permission of instructor
G (Fall)
3-0-9 units
Provides an introduction to the theory and practice of quantum computation. Topics covered: physics of information processing; quantum algorithms including the factoring algorithm and Grover's search algorithm; quantum error correction; quantum communication and cryptography. Knowledge of quantum mechanics helpful but not required.
I. Chuang, E. Farhi, S. Lloyd, P. Shor

18.436[J] Quantum Information Science
Same subject as 6.443[J], 8.371[J]
Prereq: 18.435[J]
G (Spring)
3-0-9 units
See description under subject 8.371[J].
I. Chuang

18.437[J] Distributed Algorithms
Same subject as 6.852[J]
Prereq: 6.046[J]
G (Fall)
3-0-9 units
See description under subject 6.852[J].
N. A. Lynch

18.453 Combinatorial Optimization
Subject meets with 18.4531
Prereq: 18.06, 18.700, or 18.701
Acad Year 2016-2017: U (Spring)
Acad Year 2017-2018: Not offered
3-0-9 units
Thorough treatment of linear programming and combinatorial optimization. Topics include matching theory, network flow, matroid optimization, and how to deal with NP-hard optimization problems. Prior exposure to discrete mathematics (such as 18.200) helpful. Students in Course 18 must register for the undergraduate version, 18.453.
M. X. Goemans

18.4531 Combinatorial Optimization
Subject meets with 18.453
Prereq: 18.06, 18.700, or 18.701
Acad Year 2016-2017: G (Spring)
Acad Year 2017-2018: Not offered
3-0-9 units
Thorough treatment of linear programming and combinatorial optimization. Topics include matching theory, network flow, matroid optimization, and how to deal with NP-hard optimization problems. Prior exposure to discrete mathematics (such as 18.200) helpful. Students in Course 18 must register for the undergraduate version, 18.453.
M. X. Goemans

18.455 Advanced Combinatorial Optimization
Prereq: 18.453 or permission of instructor
Acad Year 2016-2017: G (Spring)
Acad Year 2017-2018: Not offered
3-0-9 units
Advanced treatment of combinatorial optimization with an emphasis on combinatorial aspects. Non-bipartite matchings, submodular functions, matroid intersection/union, matroid matching, submodular flows, multicommodity flows, packing and connectivity problems, and other recent developments.
M. X. Goemans

Logic

18.504 Seminar in Logic
Prereq: 18.100A, 18.100B, or 18.100C; 18.06, 18.510, 18.700, or 18.701
Acad Year 2016-2017: U (Spring)
Acad Year 2017-2018: Not offered
3-0-9 units
Students present and discuss the subject matter taken from current journals or books. Topics vary from year to year. Instruction and practice in written and oral communication provided.
H. Cohn

18.510 Introduction to Mathematical Logic and Set Theory
Prereq: None
Acad Year 2016-2017: Not offered
Acad Year 2017-2018: U (Fall)
3-0-9 units
H. Cohn
18.515 Mathematical Logic
Prereq: Permission of instructor
G (Spring)
Not offered regularly; consult department
3-0-9 units

Information: B. Poonen

Probability and Statistics

18.600 Probability and Random Variables
Prereq: Calculus II (GIR)
U (Fall, Spring)
3-0-9 units. REST
Credit cannot also be received for 6.041, 6.431

Fall: J. A. Kelner
Spring: S. Sheffield

18.615 Introduction to Stochastic Processes
Prereq: 18.600 or 6.041
G (Spring)
3-0-9 units

Information: S. Sheffield

18.642 Topics in Mathematics with Applications in Finance
Prereq: 18.03; 18.06; 18.05 or 18.600
U (Fall)
3-0-9 units

Introduction to mathematical concepts and techniques used in finance. Lectures focusing on linear algebra, probability, statistics, stochastic processes, and numerical methods are interspersed with lectures by financial sector professionals illustrating the corresponding application in the industry. Prior knowledge of economics or finance helpful but not required.
P. Kemptthorne, V. Strela, J. Xia

18.650 Statistics for Applications
Subject meets with 18.6501
Prereq: 18.600 or 6.041
U (Fall, Spring)
3-0-9 units

A broad treatment of statistics, concentrating on specific statistical techniques used in science and industry. Topics: hypothesis testing and estimation. Confidence intervals, chi-square tests, nonparametric statistics, analysis of variance, regression, correlation, decision theory, and Bayesian statistics.
Fall: R. M. Dudley
Spring: P. Kemptthorne

18.6501 Statistics for Applications
Subject meets with 18.650
Prereq: 18.600 or 6.041
G (Fall, Spring)
3-0-9 units

A broad treatment of statistics, concentrating on specific statistical techniques used in science and industry. Topics: hypothesis testing and estimation. Confidence intervals, chi-square tests, nonparametric statistics, analysis of variance, regression, correlation, decision theory, and Bayesian statistics. Students in Course 18 must register for the undergraduate version, 18.650.
Fall: R. M. Dudley
Spring: P. Kemptthorne

18.655 Mathematical Statistics
Prereq: Permission of instructor
G (Spring)
3-0-9 units

Decision theory, estimation, confidence intervals, hypothesis testing. Introduces large sample theory. Asymptotic efficiency of estimates. Exponential families. Sequential analysis.
P. Kemptthorne

18.657 Topics in Statistics
Prereq: Permission of instructor
Acad Year 2016-2017: Not offered
Acad Year 2017-2018: G (Fall)
3-0-9 units
Can be repeated for credit.

Topics vary from term to term.
P. Rigollet
Algebra and Number Theory

18.700 Linear Algebra
Prereq: Calculus II (GIR)
U (Fall)
3-0-9 units. REST
Credit cannot also be received for 18.06
Vector spaces, systems of linear equations, bases, linear independence, matrices, determinants, eigenvalues, inner products, quadratic forms, and canonical forms of matrices. More emphasis on theory and proofs than in 18.06.
G. Tabuada

18.701 Algebra I
Prereq: 18.100A, 18.100B, 18.100C, or permission of instructor
U (Fall)
3-0-9 units

18.702 Algebra II
Prereq: 18.701
U (Spring)
3-0-9 units

18.703 Modern Algebra
Prereq: Calculus II (GIR)
U (Spring)
3-0-9 units
Focuses on traditional algebra topics that have found greatest application in science and engineering as well as in mathematics: group theory, emphasizing finite groups; ring theory, including ideals and unique factorization in polynomial and Euclidean rings; field theory, including properties and applications of finite fields. 18.700 and 18.703 together form a standard algebra sequence.
V. G. Kac

18.704 Seminar in Algebra
Prereq: 18.701; or 18.06, 18.703; or 18.700, 18.703
U (Fall)
3-0-9 units
Topics vary from year to year. Students present and discuss the subject matter. Instruction and practice in written and oral communication provided. Some experience with proofs required.
V. G. Kac

18.705 Commutative Algebra
Prereq: 18.702
G (Fall)
3-0-9 units
Exactness, direct limits, tensor products, Cayley-Hamilton theorem, integral dependence, localization, Cohen-Seidenberg theory, Noether normalization, Nullstellensatz, chain conditions, primary decomposition, length, Hilbert functions, dimension theory, completion, Dedekind domains.
P. I. Etingof

18.706 Noncommutative Algebra
Prereq: 18.705
Acad Year 2016-2017: G (Fall)
Acad Year 2017-2018: Not offered
3-0-9 units
Topics may include representations of quivers, Wedderburn theory, Morita equivalence, localization and Goldie’s theorem, central simple algebras and the Brauer group, maximal orders, representations, polynomial identity rings, invariant theory growth of algebras, Gelfand-Kirillov dimension.
G. Lusztig

18.708 Topics in Algebra
Prereq: 18.705
Acad Year 2016-2017: G (Fall)
Acad Year 2017-2018: Not offered
3-0-9 units
Can be repeated for credit.
Topics vary from year to year.
R. Bezrukavnikov

18.715 Introduction to Representation Theory
Prereq: 18.702 or 18.703
Acad Year 2016-2017: G (Fall)
Acad Year 2017-2018: Not offered
3-0-9 units
P. I. Etingof
18.721 Introduction to Algebraic Geometry
Prereq: 18.702, 18.901
Acad Year 2016-2017: Not offered
Acad Year 2017-2018: U (Spring)
3-0-9 units

Presents basic examples of complex algebraic varieties, affine and projective algebraic geometry, sheaves, cohomology. M. Artin

18.725 Algebraic Geometry I
Prereq: None. Coreq: 18.705
G (Fall)
3-0-9 units

Introduces the basic notions and techniques of modern algebraic geometry. Covers fundamental notions and results about algebraic varieties over an algebraically closed field; relations between complex algebraic varieties and complex analytic varieties; and examples with emphasis on algebraic curves and surfaces. Introduction to the language of schemes and properties of morphisms. Knowledge of elementary algebraic topology, elementary differential geometry recommended, but not required. R. Bezrukavnikov

18.726 Algebraic Geometry II
Prereq: 18.725
G (Spring)
3-0-9 units

Continuation of the introduction to algebraic geometry given in 18.725. More advanced properties of the varieties and morphisms of schemes, as well as sheaf cohomology. D. Maulik

18.727 Topics in Algebraic Geometry
Prereq: 18.725
Acad Year 2016-2017: G (Fall)
Acad Year 2017-2018: Not offered
3-0-9 units

Can be repeated for credit.
Topics vary from year to year. Information: D. A. Vogan

18.737 Algebraic Groups
Prereq: 18.705
Acad Year 2016-2017: G (Fall)
Acad Year 2017-2018: Not offered
3-0-9 units

Structure of linear algebraic groups over an algebraically closed field, with emphasis on reductive groups. Representations of groups over a finite field using methods from etale cohomology. Some results from algebraic geometry are stated without proof. Information: D. A. Vogan

18.745 Introduction to Lie Algebras
Prereq: 18.701 or 18.703
G (Fall)
3-0-9 units

Topics may include structure of finite-dimensional Lie algebras; theorems of Engel and Lie; Cartan subalgebras and regular elements; trace form and Cartan's criterion; Chevalley's conjugacy theorem; classification and construction of semisimple Lie algebras; Weyl group; universal enveloping algebra and the Casimir operator; Weyl's complete reducibility theorem, Levi and Maltsev theorems; Verma modules; classification of irreducible finite-dimensional representations of semisimple Lie algebras; Weyl's character and dimension formulas. G. Lusztig

18.747 Infinite-dimensional Lie Algebras
Prereq: 18.745
Acad Year 2016-2017: Not offered
Acad Year 2017-2018: G (Spring)
3-0-9 units

Topics vary from year to year. P. I. Etingof

18.748 Topics in Lie Theory
Prereq: Permission of instructor
Acad Year 2016-2017: G (Fall)
Acad Year 2017-2018: Not offered
3-0-9 units

Can be repeated for credit.
Topics vary from year to year. P. I. Etingof
18.755 Introduction to Lie Groups
Prereq: 18.100A, 18.100B, or 18.100C; 18.700 or 18.701
G (Fall)
3-0-9 units
A general introduction to manifolds and Lie groups. The role of
Lie groups in mathematics and physics. Exponential mapping.
Correspondence with Lie algebras. Homogeneous spaces and
transformation groups. Adjoint representation. Covering groups.
Automorphism groups. Invariant differential forms and cohomology
of Lie groups and homogeneous spaces. 18.101 recommended but
not required.
D. A. Vogan

18.757 Representations of Lie Groups
Prereq: 18.745 or 18.755
Acad Year 2016-2017: Not offered
Acad Year 2017-2018: G (Spring)
3-0-9 units
Covers representations of locally compact groups, with emphasis on
compact groups and abelian groups. Includes Peter-Weyl theorem
and Cartan-Weyl highest weight theory for compact Lie groups.
L. Rider

18.781 Theory of Numbers
Prereq: None
U (Spring)
3-0-9 units
An elementary introduction to number theory with no algebraic
prerequisite. Primes, congruences, quadratic reciprocity,
diophantine equations, irrational numbers, continued fractions,
partitions.
J.-L. Kim

18.782 Introduction to Arithmetic Geometry
Prereq: 18.702
Acad Year 2016-2017: U (Fall)
Acad Year 2017-2018: Not offered
3-0-9 units
Exposes students to arithmetic geometry, motivated by the problem
of finding rational points on curves. Includes an introduction to p-
adic numbers and some fundamental results from number theory
and algebraic geometry, such as the Hasse-Minkowski theorem and
the Riemann-Roch theorem for curves. Additional topics may include
Mordell's theorem, the Weil conjectures, and Jacobian varieties.
A. Sutherland

18.783 Elliptic Curves
Subject meets with 18.7831
Prereq: None. Coreq: 18.702, 18.703, or permission of instructor
Acad Year 2016-2017: U (Spring)
Acad Year 2017-2018: Not offered
3-0-9 units
Computationally focused introduction to elliptic curves, with
applications to number theory and cryptography. Topics include
point-counting, isogenies, pairings, and the theory of complex
multiplication, with applications to integer factorization,
primality proving, and elliptic curve cryptography. Includes a brief
introduction to modular curves and the proof of Fermat's Last
Theorem. Students in Course 18 must register for the undergraduate
version, 18.783.
A. Sutherland

18.7831 Elliptic Curves
Subject meets with 18.783
Prereq: None. Coreq: 18.702, 18.703, or permission of instructor
Acad Year 2016-2017: G (Spring)
Acad Year 2017-2018: Not offered
3-0-9 units
Computationally focused introduction to elliptic curves, with
applications to number theory and cryptography. Topics include
point-counting, isogenies, pairings, and the theory of complex
multiplication, with applications to integer factorization,
primality proving, and elliptic curve cryptography. Includes a brief
introduction to modular curves and the proof of Fermat's Last
Theorem. Students in Course 18 must register for the undergraduate
version, 18.783.
A. Sutherland

18.784 Seminar in Number Theory
Prereq: 18.06; 18.100A, 18.100B, or 18.100C
U (Spring)
3-0-9 units
Topics vary from year to year. Students present and discuss
the subject matter. Instruction and practice in written and oral
communication provided.
J.-L. Kim
**18.785 Number Theory I**
Prereq: None. Coreq: 18.705
G (Fall)
3-0-9 units

Dedekind domains, unique factorization of ideals, splitting of primes. Lattice methods, finiteness of the class group, Dirichlet's unit theorem. Local fields, ramification, discriminants. Zeta and L-functions, analytic class number formula. Adeles and ideles. Statements of class field theory and the Chebotarev density theorem.

A. Sutherland

**18.786 Number Theory II**
Prereq: 18.785
G (Spring)
3-0-9 units

Continuation of 18.785. More advanced topics in number theory, such as Galois cohomology, proofs of class field theory, modular forms and automorphic forms, Galois representations, or quadratic forms.

S. Raskin

**18.787 Topics in Number Theory**
Prereq: Permission of instructor
Acad Year 2016-2017: G (Fall)
Acad Year 2017-2018: Not offered
3-0-9 units
Can be repeated for credit.

Topics vary from year to year.

B. Poonen

---

**Mathematics Laboratory**

**18.821 Project Laboratory in Mathematics**
Prereq: Two mathematics subjects numbered 18.100 or above
U (Fall, Spring)
3-6-3 units. Institute LAB

Guided research in mathematics, employing the scientific method. Students confront puzzling and complex mathematical situations, through the acquisition of data by computer, pencil and paper, or physical experimentation, and attempt to explain them mathematically. Students choose three projects from a large collection of options. Each project results in a laboratory report subject to revision; oral presentation on one or two projects. Projects drawn from many areas, including dynamical systems, number theory, algebra, fluid mechanics, asymptotic analysis, knot theory, and probability.

Fall: H. R. Miller
Spring: H. Cohn

---

**Topology and Geometry**

**18.901 Introduction to Topology**
Subject meets with 18.901
Prereq: 18.100A, 18.100B, 18.100C, or permission of instructor
U (Fall, Spring)
3-0-9 units

Introduces topology, covering topics fundamental to modern analysis and geometry. Topological spaces and continuous functions, connectedness, compactness, separation axioms, and selected further topics such as function spaces, embedding theorems, dimension theory, or covering spaces and the fundamental group.

Fall: M. Hoyois
Spring: J. Hirsch

**18.9011 Introduction to Topology**
Prereq: 18.901
G (Fall, Spring)
3-0-9 units

Introduces topology, covering topics fundamental to modern analysis and geometry. Topological spaces and continuous functions, connectedness, compactness, separation axioms, and selected further topics such as function spaces, embedding theorems, dimension theory, or covering spaces and the fundamental group. Students in Course 18 must register for the undergraduate version, 18.901.

Fall: M. Hoyois
Spring: J. Hirsch

**18.904 Seminar in Topology**
Prereq: 18.901
U (Spring)
3-0-9 units

Topics vary from year to year and include the fundamental group and covering spaces. Time permitting, also covers the relationship between these objects and the theory of knots. Students present and discuss the subject matter. Instruction and practice in written and oral communication provided.

E. Dotto

**18.905 Algebraic Topology I**
Prereq: 18.701 or 18.703; 18.901
G (Fall)
3-0-9 units

Singular homology, CW complexes, universal coefficient and Künneth theorems, cohomology, cup products, Poincaré duality.

G. Tabuada
18.906 Algebraic Topology II  
Prereq: 18.905  
G (Spring)  
3-0-9 units  
Continues the introduction to Algebraic Topology from 18.905.  
Topics include basic homotopy theory, spectral sequences,  
characteristic classes, and cohomology operations.  
Information: H. R. Miller

18.917 Topics in Algebraic Topology  
Prereq: 18.906  
G (Spring)  
3-0-9 units  
Can be repeated for credit.  
Content varies from year to year. Introduces new and significant  
developments in algebraic topology with the focus on homotopy  
theory and related areas.  
G. Tabuada

18.919 Graduate Topology Seminar  
Prereq: 18.906  
G (Fall)  
3-0-9 units  
Study and discussion of important original papers in the various  
parts of algebraic topology. Open to all students who have taken  
18.906 or the equivalent, not only prospective topologists.  
H. R. Miller

18.937 Topics in Geometric Topology  
Prereq: Permission of instructor  
G (Spring)  
3-0-9 units  
Can be repeated for credit.  
Content varies from year to year. Introduces new and significant  
developments in geometric topology.  
E. Murphy

18.950 Differential Geometry  
Subject meets with 18.9501  
Prereq: 18.100A, 18.100B, or 18.100C; 18.06, 18.700, or 18.701  
U (Fall)  
3-0-9 units  
Introduction to differential geometry, centered on notions of  
curvature. Starts with curves in the plane, and proceeds to higher  
dimensional submanifolds. Computations in coordinate charts: first  
and second fundamental form, Christoffel symbols. Discusses the  
distinction between extrinsic and intrinsic aspects, in particular  
Examples such as hyperbolic space.  
X. Zhou

18.9501 Differential Geometry  
Subject meets with 18.950  
Prereq: 18.100A, 18.100B, or 18.100C; 18.06, 18.700, or 18.701  
G (Fall)  
3-0-9 units  
Introduction to differential geometry, centered on notions of  
curvature. Starts with curves in the plane, and proceeds to higher  
dimensional submanifolds. Computations in coordinate charts: first  
and second fundamental form, Christoffel symbols. Discusses the  
distinction between extrinsic and intrinsic aspects, in particular  
Examples such as hyperbolic space. Students in Course 18 must  
register for the undergraduate version, 18.950.  
X. Zhou

18.952 Theory of Differential Forms  
Prereq: 18.101; 18.700 or 18.701  
U (Spring)  
3-0-9 units  
Multilinear algebra: tensors and exterior forms. Differential forms  
on $\mathbb{R}^n$: exterior differentiation, the pull-back operation and the  
Poincaré lemma. Applications to physics: Maxwell's equations  
from the differential form perspective. Integration of forms on open  
sets of $\mathbb{R}^n$. The change of variables formula revisited. The degree  
of a differentiable mapping. Differential forms on manifolds and  
De Rham theory. Integration of forms on manifolds and Stokes'  
theorem. The push-forward operation for forms. Thom forms and  
intersection theory. Applications to differential topology.  
V. W. Guillemin

18.965 Geometry of Manifolds I  
Prereq: 18.101, 18.950 or 18.952  
G (Fall)  
3-0-9 units
18.966 Geometry of Manifolds II  
Prereq: 18.965  
G (Spring)  
3-0-9 units  
Differential forms, introduction to Lie groups, the DeRham theorem, Riemannian manifolds, curvature, the Hodge theory. 18.966 is a continuation of 18.965 and focuses more deeply on various aspects of the geometry of manifolds. Contents vary from year to year, and can range from Riemannian geometry (curvature, holonomy) to symplectic geometry, complex geometry and Hodge-Kahler theory, or smooth manifold topology. Prior exposure to calculus on manifolds, as in 18.952, is recommended.  
Fall: T. Colding  
Spring: P. Seidel

18.968 Topics in Geometry  
Prereq: 18.965  
Acad Year 2016-2017: G (Spring)  
Acad Year 2017-2018: Not offered  
3-0-9 units  
Can be repeated for credit.  
Content varies from year to year.  
W. Minicozzi

18.979 Graduate Geometry Seminar  
Prereq: Permission of instructor  
Acad Year 2016-2017: Not offered  
Acad Year 2017-2018: G (Spring)  
3-0-9 units  
Can be repeated for credit.  
Content varies from year to year. Study of classical papers in geometry and in applications of analysis to geometry and topology.  
T. Mrowka

18.999 Research in Mathematics  
Prereq: Permission of instructor  
G (Fall, Spring, Summer)  
Units arranged  
Can be repeated for credit.  
Opportunity for study of graduate-level topics in mathematics under the supervision of a member of the department. For graduate students desiring advanced work not provided in regular subjects.  
Information: A. Borodin, W. Minicozzi

18.UR Undergraduate Research  
Prereq: Permission of instructor  
U (Fall, IAP, Spring, Summer)  
Units arranged [P/D/F]  
Can be repeated for credit.  
Undergraduate research opportunities in mathematics. Permission required in advance to register for this subject. For further information, consult the departmental coordinator.  
Information: J. W. Bush

18.THG Graduate Thesis  
Prereq: Permission of instructor  
G (Fall, IAP, Spring, Summer)  
Units arranged  
Can be repeated for credit.  
Program of research leading to the writing of a Ph.D. thesis; to be arranged by the student and an appropriate MIT faculty member.  
Information: A. Borodin, W. Minicozzi

18.S096 Special Subject in Mathematics  
Prereq: Permission of instructor  
U (Fall, IAP, Spring)  
Units arranged  
Can be repeated for credit.  
Opportunity for group study of subjects in mathematics not otherwise included in the curriculum. Offerings are initiated by members of the Mathematics faculty on an ad hoc basis, subject to departmental approval. 18.S097 is graded P/D/F.  
Information: J. W. Bush
18.S995-18.S998 Special Subject in Mathematics
Prereq: Permission of instructor
G (Fall, IAP, Spring)
Units arranged
Can be repeated for credit.

Opportunity for group study of advanced subjects in mathematics not otherwise included in the curriculum. Offerings are initiated by members of the Mathematics faculty on an ad hoc basis, subject to departmental approval.

T. Arakawa